# Carbon-13 Relaxation Times of Poly(vinylnaphthalene)s in Solution

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**Synopsis.** Carbon-13 spin-lattice relaxation times and nuclear Overhauser enhancement factors were measured at 25.03 MHz and 40 °C for a solution of poly(1-vinylnaphthalene)(PlVN) and poly(2-vinylnaphthalene) (P2VN). The backbone motions in P1VN and P2VN were characterized by a distribution of correlation times. The relative mobilities of P1VN, P2VN, and polystyrene were as follows:  $\bar{\tau}_{polystyrene} < \bar{\tau}_{P2VN} < \bar{\tau}_{P1VN}$  for the average correlation times. These results were explained on the basis of the energy contour maps for polystyrene, P2VN, and P1VN.

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In our previous papers,<sup>1-3)</sup> we explained the conformational characteristics of poly(1-vinylnaphthalene) (P1VN) and poly(2-vinylnaphthalene) (P2VN), by estimating the steric compression energies of the rotational isomeric states (RIS) of the naphthyl side groups and the conformational energies of the skeletal bonds.

The revealed differences of the characteristics between P1VN and P2VN corresponded well with the difference of the solution properties of P1VN and P2VN, such as in transition<sup>1)</sup> phenomenon, NMR spectra patterns<sup>2)</sup> and in fluorescence spectra of the solution.<sup>3)</sup>

Futhermore, some information about the molecular dynamics of PIVN and P2VN can be also drawn from the previous calculations. The segmental motion of PIVN chain may undergo the steric restriction of the neighboring 1-naphthyl groups. Since the P2VN chain is not so spatially crowded by neighboring 2-naphthyl groups as the chain in PIVN is, the motion of the main chain in the former would not be so influenced by the restriction of neighboring groups. Consequently, the relative mobilities of PIVN, P2VN, and polystyrene chains can be predicted as follows:  $\tau_{polystyrene} < \tau_{p2VN}$  $<\tau_{PIVN}$  for the correlation time  $\tau$ . These correlation times can be estimated by the measurement o carbon-13 spin relaxation time and nuclear Overhauser enhancement. The purpose of this paper is to discuss the segmental motion in PIVN and P2VN chain as characterized by a distribution of the correlation times.

### **Experimental**

Samples of P1VN and P2VN were prepared by radical polymerization, using a,a'-azobisisobutyronitrile as an initiator. The number-average molecular weights of these polymers were determined using a "KUNAUAR's Membrance Osmometer" in chloroform solution at 37 °C. The average molecular weights of P1VN and P2VN were  $4.0\times10^4$  and  $7.5\times10^4$ , respectively. In the vinyl aromatic polymers with this range of the degree of polymerization, the  $T_1$  values are almost independent of the chain lengths.<sup>4,5)</sup>

Natural abundance  $^{13}$ C NMR spectra were obtained at 25.03 MHz by Fourier transform techniques using a JEOL JNM PS-100 spectrometer; details described before. Spinlattice relaxation times  $T_1$  were measured from PRFT spectra obtained from 180°-t-90° sequences. The spectra of the polymer solutions of ca. 30% concentrations in dioxane- $d_8$  were observed at 40 °C. Nuclear Overhauser enhancements (NOE)

were measured by comparison of coupled and decoupled spectra. The maximum errors in  $T_1$  and NOE were within  $\pm 10\%$ .

## Calculation

Assuming only the dipolar interactions between a methine carbon and the proton bonded to it, the  $^{13}$ C  $T_1$  and NOEF (NOE-1) are given by  $^{6,7)}$ 

$$1/T_1 = 2.190 \times 10^9 (f(\omega_1) + 3f(\omega_2) + 6f(\omega_3)) \text{ s}^{-1}, \tag{1}$$

NOEF = 
$$\frac{(-f(\omega_1) + 6f(\omega_2))}{(f(\omega_1) + 3f(\omega_2) + 6f(\omega_3))} \times 3.976,$$
 (2)

$$\omega_1 = \omega_H - \omega_C, \tag{3}$$

$$\omega_2 = \omega_C,$$
 (4)

and

$$\omega_3 = \omega_H + \omega_C, \tag{5}$$

where  $\omega_{\rm c}$  and  $\omega_{\rm H}$  are the Larmor frequencies for <sup>13</sup>C and <sup>1</sup>H, respectively and for <sup>13</sup>C measurement at 25.03 MHz,  $\omega_1$ =4.682×10<sup>8</sup> rad s<sup>-1</sup>,  $\omega_2$ =1.573×10<sup>8</sup> rad s<sup>-1</sup>,  $\omega_3$ =7.828×10<sup>8</sup> rad s<sup>-1</sup>. As the backbone motion in a polymer is characterized by a distribution of correlation times, the spectral density function  $f(\omega_i)$  is written by considering a log  $-\chi^2$  distribution,<sup>8,9)</sup> as follows:

$$f(\omega_i) = \frac{\bar{\tau} \Gamma^{(p)}(s)(b^s - 1) ds}{(b - 1)(1 + \omega_i^2 \bar{\tau}^2((b^s - 1)/(b - 1))^2)}$$
(6)

$$\Gamma^{(p)}(s) = \frac{1}{\Gamma(p)} (ps)^{p-1} \exp(-ps) p ds, \tag{7}$$

and

$$s = \log_b(1 + (b-1)\tau/\bar{\tau}) \tag{8}$$

where  $\Gamma$  function,  $\Gamma(p)$ , normalizes  $\Gamma^{(p)}(s)$  to unity, and the width of the distribution is characterized by p. The value of log base b=1000 is used. The  $\bar{\tau}$  represents an average correlation time. Using Eqs. 1—8,  $T_1$  and NOEF were computed by varying the width parameter p from 1 to 100 in 1-unit steps, and by varying the average correlation time  $\bar{\tau}$  from  $1.0 \times 10^{-7}$  to  $1.0 \times 10^{-12}$  s<sup>-1</sup>

# Results and Discussion

The proton-decoupled  $^{13}$ C NMR spectra of PlVN and P2VN at 40  $^{\circ}$ C are shown in Figs. 1a and b, respectively. The signal peaks of naphthyl carbons are denoted by the symbols A, B, C, D, E, and F from the order of the low magnetic field. Table 1 shows the  $^{13}$ C  $T_1$  values for the aromatic peaks in PlVN and P2VN, together with those for polystyrene reported in the literature.  $^{5,10,11)}$  The  $T_1$  for the aromatic carbons suggests that A–C peaks correspond to the nonprotonated carbons, and that D–F for PlVN and D, E for P2VN correspond to the protonated carbons. The line widths of A peaks in PlVN and P2VN are somewhat broader than that of B or C peak. Since this feature is attributed

TABLE 1	13C SPIN-LATTICE RELAXATION TIMES OF AROMATIC CARBON IN	J PIVN	P2VN AN	ID POLVSTVDENE

Polymer	Solvent	Temp/°C	Aromatic carbons $T_1$ /ms					
			Α	В	C	D	E	F
PIVN	$\text{Dioxane-}d_8$	40	968	1320	1520	78	85	86
P2VN	Dioxane- $d_8$	40	928	1380	1440	91	84	
		_	Meta, ortho carbon		Para carbon		Ref.	
Atactic polystyrene	Toluene- $d_8$	30	140		120		10	
Atactic polystyrene	Tetrachloroethylene	44	98		8 89		5	
Atactic polystyrene	Tetramethylene oxide	30		126		11	0	11

Table 2.  $^{13}\text{C}$  Spin-lattice relaxation times and NOE of methine carbon in P1VN, P2VN, and polystyrene in solution

Polymer	Solvent	Temp/°C	$T_1/\mathrm{ms}$	NOE	$ar{ au}/\mathrm{s}^{-1}$	þ	Ref.
PIVN	Dioxane-d <sub>8</sub>	40	66	1.40	$1.6 \times 10^{-8}$	20	
P2VN	$\text{Dioxane-}d_8$	40	64	1.70	$5.3 \times 10^{-9}$	12	
Isotactic polystyrene	o-Dichlorobenzene	35	65	1.80	$1.0 \times 10^{-9}$	18	9
Atactic polystyrene	Pentachloroethane	30			$4.5 \times 10^{-9}$	20	12

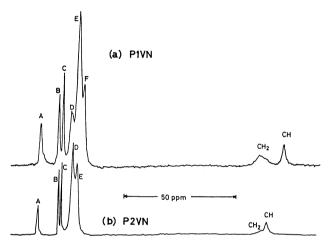


Fig. 1. Proton-decoupled, natural abundance  $^{13}$ C FT NMR spectra of (a) P1VN and (b) P2VN in dioxane- $d_8$  at 25.03 MHz and 40 °C.

to the tacticity number in the polymer samples used, the A peak can be assigned to the naphthyl carbons, which bond to  $\alpha$ -carbon. A similar phenomenon was observed in polystyrene. The other peaks of the aromatic carbons can not be assigned to each carbon in the naphthyl group at the present stage.  $T_1$  values of the protonated carbon in P1VN and P2VN are smaller than that of polystyrene. This observation suggests that the naphthyl ring rotation is perturbed by the neighboring naphthyl rings, CH and CH<sub>2</sub> groups.

The average correlation times  $\bar{\tau}$  and width parameter p satisfying the observed values ( $T_1$  and NOE) are given in Table 2.  $T_1$  value of methine carbon in P1VN was approximately equal to that of P2VN or polystyrene. It is apparent that the correlation time can not be adequately approximated by the  $T_1$  value, and the  $\bar{\tau}$  values for the segmental motion of these polymer are mainly influenced by the NOEF.

The segmental motion of PlVN was estimated to be slower than that for P2VN and polystyrene, as was

expected. The order of the relative mobilities of the polymer chains agreed with that described above. These experimental results are explained as follows. The mobility of the main chain would be correlated to the values of the contour lines of the energy maps, which surround all the minima (tt, gt, tg, and gg) positions, since the energy value of each contour has a influence upon the magnitude of the change in RIS (t and g) of the molecular chain. In a previous paper,3) all minima in the conformational energy maps of PIVN chain were shown to be surrounded by the contour lines of 9 kcal mol-1,† in the P2VN chain, the lines were 7-8 kcal mol<sup>-1</sup>, while in polystyrene, it was sufficient to surround the all minima by contours of 5— $6 \text{ kcal mol}^{-1}$ . The order of the energy of these contours was found to be that of the chain mobilities described above.

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<sup>†:</sup> In SI units: 1 kcal mol<sup>-1</sup>=4.184 kJ mol<sup>-1</sup>.